Doping evolution of the chemical potential, spin-correlation gap, and charge dynamics of Nd$_{2-x}$Ce$_x$CuO$_4$

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We report an optical reflectivity study on Nd$_{2-x}$Ce$_x$CuO$_4$ over a broad doping range 0 ≤ x ≤ 0.20. The study reveals a systematic shift of the chemical potential with doping. A pronounced peak structure specific to the electron-doped cuprate is observed in the optical scattering rate based on the extended Drude model analysis. The energy scale of the peak could be very different from that of the peak in conductivity spectrum. We clarify that the “hot spots” gap probed in photoemission experiments is more closely related to the sharp suppression feature in scattering rate than in conductivity spectra. The gap is associated with the short-range antiferromagnetic correlation, and disappears in a manner of fading away with increasing doping and temperature. In the heavily overdoped region, a dominant ω$^2$-dependence of the scattering rate is identified up to very high energy.

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I. INTRODUCTION

A central issue in understanding the mechanism of high-temperature superconductivity is how an antiferromagnetic (AF) insulator evolves into a superconductor with electron or hole doping. Although both the electron- and hole-doped high-$T_c$ superconductors share many similarities, including the $d$-wave pairing symmetry, their phase diagrams exhibit rather asymmetric behaviors.$^1$ For the hole-doped cuprates, the AF order disappears with a small amount of carrier concentration, and the superconducting phase is well-separated from the AF ordered phase; while in the electron-doped cuprates, the AF order is much more robust with respect to doing, and the AF and superconducting phases are adjacent to each other or even coexist. The doping range where the superconducting transition occurs in the electron-doped cuprates is narrower and the maximum $T_c$ is lower than those in the hole doped cuprates. Angle-resolved photoelectron spectroscopy (ARPES) experiments indicated that the hole carriers doped into the parent compound first enter $(\pi/2, \pi/2)$ points in the Brillouin zone and produce a Fermi arc.$^2$ By contrast, for the electron-doped case, a small Fermi surface pocket appears first around $(\pi, 0)$, and another one shows up around $(\pi/2, \pi/2)$ upon increasing doping. The two pockets are separated by a gaped region located at the intersecting points (so-called “hot spots”) of the Fermi surface and the AF zone boundary.$^3$

Optical spectroscopy can probe not only the low-lying intraband response, but also the interband transitions from occupied to unoccupied states. It provides supplementary information about the electronic states as yielded by ARPES, which detects only occupied states. Previous optical studies on the Nd$_{2-x}$Ce$_x$CuO$_4$ (NCCO) system$^4$-$^7$ have uncovered a transfer of spectral weight from charge-transfer excitations to low frequencies with doping, and an occurrence of a large pseudogap in optical conductivity, which is believed to be a reflection of the gaped region in the Fermi surface seen in ARPES experiment. A recent doping-dependent optical study further suggested that this partial gap is associated with an ordered phase which ends on a quantum critical point at approximately optimal doping.$^8$ In this paper, we present a more systematic optical study on NCCO single crystals. Our samples cover a very broad doping range from the parent compound to the overdoped nonsuperconducting compound. The study reveals a number of properties, including a systematic shift of chemical potential, a spin-correlation gap which fades away with doping/temperature with no clear phase boundary line, and a dominant ω$^2$-dependence of the scattering rate up to very high energy in the nonsuperconducting overdoped region. We clarify that the “hot spots” gap probed in ARPES experiments correlates with the gap in the scattering rate spectrum better than with the suppression feature in optical conductivity spectrum.

II. EXPERIMENTS

The NCCO single crystals were grown from a copper-oxide-rich melt in Al$_2$O$_3$ crucibles over a wide range of Ce concentration 0 ≤ x ≤ 0.20. The actual Ce concentration was determined by inductively coupled plasma spectrometry analysis experiments, and by energy-dispersive x-ray analysis using scanning electron microscopy, respectively. All samples were annealed in flowing helium for over 10 h at 900 °C to remove the interstitial oxygen.

The near-normal incident reflectance spectra [R(ω)] were measured by a Bruker 66v/s spectrometer in the frequency range from 50 to 25,000 cm$^{-1}$. The crystal with a very shiny surface was mounted on an optically black cone in a cold-finger flow cryostat. An in situ gold and aluminum overcoating technique was employed for reflectance measurements.$^9$ The optical conductivity spectra were obtained from Kramers-Kronig transformation of $R(\omega)$. We use Hagen-
been observed previously and shares many similarities with further doping. Such spectral change has first at low doping, then a Drude component appears at lower frequencies with increasing doping. A midinfrared broad peak at about 4000–5000 cm$^{-1}$ is formed from charge-transfer excitations to low frequency occurs. A lines. Upon Ce substitution, a transfer of spectral weight also shifts gradually to higher frequencies with increasing doping. Similar shift is visible in previous measurements. As elaborated below, this behavior is mainly associated with the change of chemical potential with electron doping.

It is useful to compare the above result with ARPES data first. ARPES measurement on undoped Nd$_{2-x}$Ce$_x$CuO$_4$ revealed a dispersion band $\sim$1.3 eV below the chemical potential $\mu$ along zone diagonal, which was ascribed to the oxygen-derived charge transfer band. Note that this energy (1.3 eV) is lower than the charge-transfer excitation ($\sim$1.5 eV) seen in optical measurement. As we mentioned, ARPES experiment detects the occupied states relative to the chemical potential, while optics probes the interband transition from an occupied band below $\mu$ to another unoccupied band above $\mu$. The small difference between the two probes indicates that $\mu$ locates just slightly below the Cu 3$d$ upper Hubbard band in Nd$_2$CuO$_4$ (Fig. 2). By contrast, $\mu$ for the hope-type parent compound La$_2$CuO$_4$ is close to the oxygen 2$p$ band. This is because the dispersive band seen in ARPES measurement is not far from the Fermi level, while the charge-transfer excitations probed by optical measurement are around 2 eV. The fact that $\mu$ is very close to the Cu 3$d$ upper Hubbard band in Nd$_2$CuO$_4$ and to the O 2$p$ band in La$_2$CuO$_4$ explains why electrons and hole are easily doped into those different types of compounds, respectively.

There exists a long standing controversy over the evolution of $\mu$ with doping in cuprates. One simple picture is that $\mu$ moves into the valence or conduction band as the material is doped away from the half filling with holes or electrons, respectively. Another opinion is that carrier doping creates “states” inside the insulating gap, but $\mu$ remains relatively fixed in the middle of the gap. It is difficult to get to a definite solution to this issue solely from APRES measurement. In fact, the experimental data on different materials have been interpreted in terms of both scenarios. The present optical experiments, showing a shift of charge-transfer excitation with doping, can be naturally explained by assuming that $\mu$ enters the upper Cu 3$d$ Hubbard band and shifts up with electron doping. As illustrated in Fig. 2, when the chemical potential moves into the conduction band, some states in the Cu 3$d$ upper Hubbard band are occupied, then the charge-transfer transition from the oxygen 2$p$ band to the unoccupied part of the Cu 3$d$ upper Hubbard band will require higher energy. Obviously, this transition energy increases with further doping. The chemical potential shift in NCCO was also seen in a core-level photoemission study. The present study provides optical evidence for the shift.

Before moving on to other issues, we make comments on possible arguments or questions which may challenge the above analysis. One argument is that the optical transition does not alter the total electron number in a system, therefore the optical spectroscopy cannot be a direct probe of the chemical potential. We remark that this argument wrongly mixes the concept of the change of carrier number in a sys-
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...tem controlled by doping with whether an experimental probe can alter the total carrier number of a system. As the doping level changes, the carrier number of a system will change accordingly, which could lead to the shift of the chemical potential. Our above analysis indicates that the optical spectroscopy can probe the interband transition energy which in turn yields information about the chemical potential shift. We emphasize that the optical spectroscopy does not measure the absolute value of the chemical potential, but offers information about the relative position of the chemical potential with respect to the conduction band.

Another argument is that the shift of the charge-transfer excitation peak is not solely originated from the chemical potential shift, it could be also due to the band shift caused by the gradual substitution of Ce for Nd ions. Indeed, the charge-transfer energy gaps (or Mott-Hubbard gaps in the case of Mott-Hubbard insulators) could be significantly different for compounds with different ions either in the rare-earth sites or transition-metal sites. Interpretations for such difference have been made based on different models and scenarios. In general, the values of the charge-transfer gaps (or Mott-Hubbard gaps) depend on the effective correlation strength, i.e., the ratio of the bandwidth \( W \) to the Hubbard repulsion energy \( U \). A strong/weak effective correlation strength results in a large/small gap value. However, it should be noted that the charge-transfer excitations in Nd2−CeCuO4 studied in this work shift in an opposite way. The system evolves from an AF charge-transfer insulator (parent compound) to a metal (superconductor) upon doping, and tends to become Fermi-liquid-like in the heavily overdoped region. It is well-known that the effective correlation strength decreases with doping in the cuprate systems. On the contrary, the charge-transfer excitations observed above shift to higher energy, opposite to the trend expected from the decrease of the effective correlation strength. This leads us to conclude that the dominant effect must be the shift of the chemical potential, although the change of band structure with doping may be present.

IV. EVOLUTION OF “HOT SPOTS” GAP

A. Gap features in conductivity and scattering rate spectra

Figure 3 shows the \( T \)-dependent \( R(\omega) \) spectra for several doping levels \( x=0.06, 0.10, 0.14, \) and 0.20, respectively. The \( x=0.06 \) and 0.10 samples are heavily underdoped and located below the superconducting region, the \( x=0.14 \) sample is slightly underdoped with \( T_c \approx 18 \) K, while the \( x=0.20 \) sample is highly overdoped and also out of the superconducting region in the phase diagram. The most prominent feature is a reverse S-shape at low \( T \) for the underdoped samples. Correspondingly, the conductivity spectra, displayed in the upper panels of Fig. 4, show suppressions of spectral weight below \( \sim 0.5 \) eV \( (4000 \ \text{cm}^{-1}) \). Such behavior was observed in previous optical measurement and referred to as a pseudogap. The suppressions are clearly seen for \( x=0.06 \) and 0.10 samples, and are also present in the low-\( T \) curves for the \( x=0.14 \) superconductor. In the meantime, Drude-like peaks are still seen at very low frequency for all those samples, evidencing metallic responses in both \( T \)- and \( \omega \)-dependences. Those observations indicate clearly that the gap appears only on parts of the Fermi surface. The Drude-type contribution originates from the gapless regions of the Fermi surface.

The dynamics of charge carriers is usually described in terms of frequency-dependent scattering rate on the basis of the extended Drude model,

\[
\frac{1}{\tau(\omega)} = \frac{\omega_p^2}{4\pi} \text{Re} \frac{1}{\sigma(\omega)},
\]

where \( \sigma(\omega) = \sigma_r(\omega) + i\sigma_i(\omega) \) is the complex conductivity, and \( \omega_p \) is the plasma frequency which can be obtained by sum-merizing \( \sigma_r(\omega) \) up to the reflectance edge frequency. The scattering rate spectra for the above four samples are shown in the bottom panels of Fig. 4. Related to the suppression in \( \sigma_r(\omega) \) spectrum, we observe a peak in \( 1/\tau(\omega) \) for under-doped Nd2−CeCuO4 samples, below which the scattering rate is strongly suppressed.

It should be noted that a depression of \( 1/\tau(\omega) \) at low frequencies followed by a peak or overshoot at high frequencies is also a characteristic feature for a gaped state. To explain such a structure, Basov et al. introduced an approximate sum rule for the difference between energy-dependent scattering rates:

\[
\int_0^{\omega_p} d\omega \left( \frac{1}{\tau^A(\omega)} - \frac{1}{\tau^B(\omega)} \right) = 0,
\]

where indexes \( A \) and \( B \) refer to different states of the studied system (e.g., normal, pseudogap, superconducting). This sum rule is based on the exact value of the imaginary part of the loss function,

\[
\int_0^{\infty} \frac{d\omega}{\omega} \text{Im}[\epsilon^{-1}(\omega, T)] = -\frac{\pi}{2}.
\]

In the case of \( \omega < \omega_p \), the scattering rate can be expressed as \( 1/\tau(\omega) \approx \omega_p^{-1} \text{Im}(1/\epsilon) \) and therefore the sum rule is obeyed. According to Eq. (2), the suppression of \( 1/\tau(\omega) \) in the intragap region ought to be balanced out by the overshoot at \( \omega > E_g \). Indeed, such a characteristic structure, i.e., a decrease and then an overshoot in \( 1/\tau(\omega) \), was found to be...
present in the materials with development of different sorts of gaps. For example, the behaviors were seen in antiferromagnet Cr where a spin-density-wave (SDW) gap opens on parts of the Fermi surface,\textsuperscript{16} and in the heavy-fermion materials YbFe\textsubscript{4}Sb\textsubscript{12} and UPd\textsubscript{2}Al\textsubscript{3} where hybridization gaps due to the mixing of the $f$ band and the conduction band open on parts of the Fermi surface.\textsuperscript{16,17}

In high-$T_c$ cuprates, the effect of the formation of a superconducting gap or the development of a pseudogap on the scattering rate is more complicated. For hole-type cuprates, due to the fact that the in-plane carrier dynamics is governed by the nodal region of the Fermi surface that remains gapless at all temperatures, the gap effect is usually very weak. For optimally doped YBCO\textsuperscript{16} and Tl-based systems,\textsuperscript{18} a small overshoot shows up immediately above the suppression in $1/\tau(\omega)$ in the superconducting state. However, for underdoped cuprates, particularly in the pseudogap state, the overshoot is usually not observed, the spectral weight lost at low $\omega$ is not recovered up to the highest frequency measured. A thorough discussion about the respective effects of superconducting gaps with $s$-wave and $d$-wave symmetries on the sum rules for $1/\tau(\omega)$ was provided by Marsiglio et al.\textsuperscript{19} Nevertheless, for the electron-doped compounds under present investigation, the $1/\tau(\omega)$ spectra display significant peak structures just above the suppressions. The energy scale of the peak is much higher than that of the small overshoot below $T_c$ in $1/\tau(\omega)$ for hole-type cuprates at the optimal doping. Therefore this structure is specific to the electron-doped cuprates. It provides strong evidence for the gap formation on the Fermi surface in the underdoped NCCO. Apparently, the gaps in the present case are not superconducting ones, but correspond to the gaps at “hot spots” with a much larger energy scale. Since the “hot spots” locate at the intersecting points of the Fermi surface and the AF zone boundary, the gap is attributed to the strong AF spin correlation. Therefore the gap has a spin-density-wave (SDW) type origin, being consistent with earlier studies.\textsuperscript{7,8} As the hot spots are closer to the nodal region in the electron-doped cuprates, the gap features appear more pronounced.

**B. Different energy scales for the peaks in $\sigma_1(\omega)$ and $1/\tau(\omega)$ and their evolutions with doping**

We notice that the peak positions in $1/\tau(\omega)$ spectra can be quite different from the peak positions in $\sigma_1(\omega)$ spectra. For example, in the $x=0.06$ sample, the peak in $\sigma_1(\omega)$ locates near 4000 cm$^{-1}$, while the peak in $1/\tau(\omega)$ is only around 2000 cm$^{-1}$. A natural question is which one reflects the gap amplitude? Previously, the pseudogap observed in optics and its connection with the gap seen in ARPES was established from $\sigma_1(\omega)$ spectra,\textsuperscript{7} but this should be reexamined.

It is worth mentioning that there is no simple and direct connection between the quantity $\sigma_1(\omega)$ or $1/\tau(\omega)$ and the density of states (DOS). In order to know the gap magnitude, one needs a model to derive those optical quantities which, in general, involve a summation over the full Fermi surface. As there is no theoretical study available for distinguishing the gap features in the two optical quantities, we consider a special case here. We calculate the conductivity spectra for a standard BCS model with an energy gap of $2\Delta$ in both clean and dirty limits for $T \ll T_c$.\textsuperscript{20} then determine $1/\tau(\omega)$ from the extended Drude model [Eq. (1)]. The model should be applicable to both the superconducting and the CDW/SDW gaps. The results are shown in Fig. 5. The calculation well reproduces the sharp peak structure near $2\Delta$ in $1/\tau(\omega)$ as obtained by Basov et al.,\textsuperscript{16} which is due to the presence of a singularity of DOS. It clearly indicates that, for the same strength of impurity scattering, the peak position in $\sigma_1(\omega)$ could be very different from that in $1/\tau(\omega)$, although both can occur above the gap energy. The peak in $\sigma_1(\omega)$ always appears at a higher energy. But the energy difference between the peaks in $\sigma_1(\omega)$ and $1/\tau(\omega)$ becomes smaller with reducing the impurity scattering due to a faster shift of the peak position towards the low frequency in $\sigma_1(\omega)$. On this account, the gap energy is much closer to the peak energy in $1/\tau(\omega)$ than that in $\sigma_1(\omega)$.

Although the calculations are for the case of a fully gapped Fermi surface, the experimental data for the “hot spot” gaps of NCCO (i.e., partial gaps in the Fermi surface) qualitatively follow the trend both in the peak positions and

![Figure 4](184502-4.png)
Another important feature is that, when the pseudogap goes away by further increasing doping, the $1/\tau(\omega)$ indicates a dominant $\omega^{2}$-dependence [see the $1/\tau(\omega)$ spectra for the $x=0.20$ sample in Fig. 4], suggesting a Fermi liquid-like state. The $1/\tau(\omega)$ spectra of the $x=0.14$ sample deviate from such $\omega^{2}$-dependence at the low frequency even at room temperature, suggesting that the short-range AF correlation is still effective at this doping level and temperature range. We believe that, at the heavily overdoped region, due to the disappearance of the AF correlation, the magnetic folding of the Fermi surface vanishes completely, consequently, a single large Fermi surface centered at $(\pi, \pi)$ is formed. The amazing observation is that this $\omega^{2}$-dependence goes up to the very high frequency, beyond 6000 cm\(^{-1}\) as shown in Fig. 4. This is very different from the hole-doped cuprates. In the hole-doped case, the scattering rate follows a linear $\omega$-dependence which is well-described by the marginal Fermi liquid theory, whereas at high frequencies (around 0.5 eV) a saturation of $1/\tau(\omega)$ is commonly observed.\(^{24}\)

Finally, we remark that we employ the extended Drude mode, the so-called one-component approach, to the data from very underdoped to overdoped samples 0.06$\leq x \leq 0.20$. The purpose is to show the spectral evolution with doping and to display the gross features in both $\sigma_{1}(\omega)$ and $1/\tau(\omega)$ spectra. Such one-component approach is commonly used for hole-doped cuprates near the optimal doping, which yields a linear frequency dependent $1/\tau(\omega)$. For underdoped samples, for example, YBa\(_{2}\)Cu\(_{3}\)O\(_{y}\) with $y \leq 6.5$, a nonmonotonic form of $1/\tau(\omega)$ with a negative slope at high $\omega$ was observed.\(^{25}\) The negative slope in $1/\tau(\omega)$ clearly indicates the breakdown of such one-component approach. Here we found that the electron-doped system shows a very different behavior in $1/\tau(\omega)$. As seen from Fig. 4, even for the very underdoped samples, the $1/\tau(\omega)$ spectra exhibit positive slopes at high $\omega$. The peak (or the very pronounced overshoot) just above the suppression in $1/\tau(\omega)$ is originated from the gap at the hot spots, as we elaborated above. Additionally, we would like to remark that the structure in $1/\tau(\omega)$ of Fig. 4 could not be caused by the coupling of charge carriers with a bosonic mode. As discussed in detail in Refs. 26 and 27, although the mode coupling can lead to a sharp increase feature (or depression when looking from the high-frequency side) near the mode frequency in $1/\tau(\omega)$, it can never cause an overshoot/peak in $1/\tau(\omega)$. Even for a very weak overshoot structure, a gap in the density of state has to be included in order to well reproduce the curve structure.

V. SUMMARY

Our systematic study on the NCCO crystals reveals a number of properties: (1) The chemical potential is not pinned in the gap region, but shifts up with electron doping. (2) Both the $\omega$-dependent conductivity and scattering rate spectra exhibit characteristic structures caused by the “hot spots” gaps in the Fermi surface for underdoped samples. The peak position in $1/\tau(\omega)$ is found to be quite different from the one in $\sigma_{1}(\omega)$. We clarify that the “hot spots” gap probed by ARPES experiments correlates directly with the

FIG. 5. (Color online) The calculated conductivity and scattering rate spectra for a BCS model ($T \ll T_{c}$) in both the clean and dirty limits with $(1/\tau)/\Delta = 1, 2, \text{and } 20$. With doping evolution. Since the electrons in heavily underdoped samples experience stronger scattering, a larger energy difference between those peaks was observed, as one would expect. Additionally, the gap magnitude in $1/\tau(\omega)$ is indeed comparable to the gap energy at “hot spots” seen in ARPES measurement. Matsui et al. recently measured the $T$-dependent ARPES spectra on a NCCO crystal at $x=0.13$,\(^{21}\) and identified a maximum gap (i.e., a hump feature in an energy dispersion curve) $\sim 0.19$ eV. This value is very close to the peak positions in $1/\tau(\omega)$ for the compounds with similar Ce contents.

We now address the evolution of the AF gap with doping. From Fig. 4, we found that the peak in $1/\tau(\omega)$ shows much less frequency shift than the suppression feature in $\sigma_{1}(\omega)$ with increasing doping. The most prominent change is a weakening of the gap structure with increasing doping and temperature. The results suggest that the disappearance of the gap feature is not due to the reduction of the gap energy, but in a manner of gradually fading away. The result is in good agreement with Raman scattering experiment on the two-magnon peak: its intensity decreases with Ce doping but the peak energy shows little doping dependence.\(^{7}\) ARPES data on the underdoped Nd\(_{1.85}\)Ce\(_{0.15}\)CuO\(_{4}\) further indicated that the AF pseudogap was gradually filled up with increasing $T$ without showing any observable shift in energy.\(^{21}\) Note that although the gap is due to the AF scattering,\(^{22}\) it opens at a temperature much higher than the AF ordered Neel temperature $T_{N}$ and in a doping region where there is no long range AF ordering. Clearly, the gap already shows up when the short range AF correlation exists. Unlike the AF long range order which has a definite phase transition temperature, the AF short range order is a gradually evolving behavior with no phase line as a function of doping. Some authors suggest the existence of a quantum phase transition in the phase diagram for the electron-doped cuprates.\(^{8,23}\) However, our analysis above suggests that the gap feature is associated with the short range AF interaction, with no clear boundary line or any critical point.
suppression feature in $1/\tau(\omega)$ rather than in optical conductivity spectra. (3) The gap becomes weaker with increasing doping/temperature and disappears in a manner of fading away. There is no clear phase transition line for the gap vanishing. (4) In the heavily overdoped region, the gap structure disappears completely due to the absence of the AF correlation, and a single large Fermi surface should be formed. We identify a $\omega^2$-dependence of $1/\tau(\omega)$ up to very high energy with no indication of saturation.

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15See, for example, the review article I. Imada, A. Fujimori, and Y. Tokura, Rev. Mod. Phys. 70, 1039 (1998), and references therein.